

Five derivative rules for operations on functions.

Constant Multiple Rule: $\frac{d}{dx} [cf(x)] = cf'(x)$

Sum and Difference Rule: $\frac{d}{dx} [f(x) \pm g(x)] = f'(x) \pm g'(x)$

Product Rule: $\frac{d}{dx} [f(x) \cdot g(x)] = f'(x)g(x) + f(x)g'(x)$

Quotient Rule: $\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2}$

Chain Rule: $\frac{d}{dx} [f(g(x))] = f'(g(x)) \cdot g'(x)$

Ten derivative rules for functions

Derivative of a Constant: $\frac{d}{dx} [c] = 0$, where c is a constant.

The Power Rule: $\frac{d}{dx} [x^n] = nx^{n-1}$

Exponential Functions: General Case: $\frac{d}{dx} [a^x] = a^x \cdot \ln(a)$

Exponential Functions: Special Case: $\frac{d}{dx} [e^x] = e^x$

Three Trigonometric Rules. $\frac{d}{dx} [\sin(x)] = \cos(x)$

$$\frac{d}{dx} [\cos(x)] = -\sin(x)$$

$$\frac{d}{dx} [\tan(x)] = \sec^2(x) = \frac{1}{\cos^2(x)}$$

Three Inverse Function Rules

$$\frac{d}{dx} [\ln(x)] = \frac{1}{x}$$

$$\frac{d}{dx} [\arctan(x)] = \frac{1}{1+x^2}$$

$$\frac{d}{dx} [\arcsin(x)] = \frac{1}{\sqrt{1-x^2}}$$

General Antiderivative Rules

If k is a constant $\int k dx = kx + C$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \text{ when } n \neq -1$$

$$\int a^x dx = \frac{a^x}{\ln(a)} + C$$

$$\int e^x dx = e^x + C$$

$$\int \cos(x) dx = \sin(x) + C$$

$$\int \sin(x) dx = -\cos(x) + C$$

$$\int \sec^2(x) dx = \tan(x) + C$$

$$\int \frac{1}{x} dx = \ln(|x|) + C$$

$$\int \frac{1}{1+x^2} dx = \arctan(x) + C$$

$$\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin(x) + C$$